The formulas of a standard helical rack are similar to those of **Table 6-6** with only the normal coefficient of profile shift $x_n = 0$. To mesh a helical gear to a helical rack, they must have the same helix angle but with opposite hands.

The displacement of the helical rack, l, for one rotation of the mating gear is the product of the radial pitch, p_t, and number of teeth.

$$l = \frac{\pi m_n}{\cos\beta} z = p_t z \qquad \textbf{(6-13)}$$

According to the equations of **Table 6-7**, let radial pitch p_t = 8 mm and displacement l = 160 mm. The radial pitch and the displacement could be modified into integers, if the helix angle were chosen properly.

In the axial system, the linear displacement of the helical rack, l, for one turn of the helical gear equals the integral multiple of radial pitch.

$$l = \pi z m_t \qquad \textbf{(6-14)}$$

SECTION 7 SCREW GEAR OR CROSSED HELICAL GEAR MESHES

These helical gears are also known as spiral gears. They are true helical gears and only differ in their application for interconnecting skew shafts, such as in **Figure 7-1**. Screw gears can be designed to connect shafts at any angle, but in most applications the shafts are at right angles.

7.1 Features

7.1.1 Helix Angle And Hands

The helix angles need not be the same. However, their sum must equal the shaft angle:

$$\beta_1 + \beta_2 = \Sigma \qquad \textbf{(7-1)}$$

where β_1 and β_2 are the respective helix angles of the two gears, and Σ is the shaft angle (the acute angle between the two shafts when viewed in a direction paralleling a common perpendicular between the shafts).

Except for very small shaft angles, the helix hands are the same.

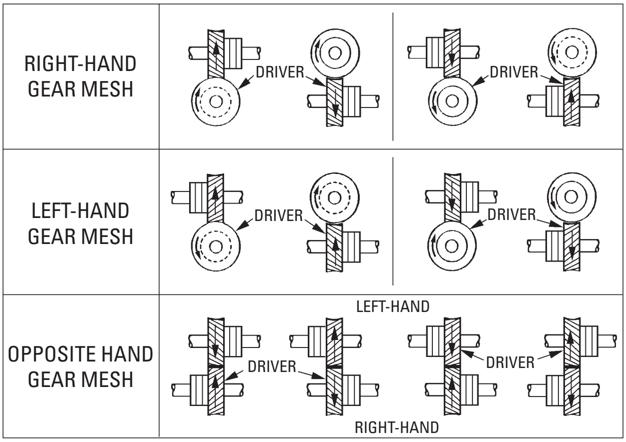

Fig. 7-1 Types of Helical Gear Meshes

NOTES:
1. Helical gears of the same hand operate at right angles.
2. Helical gears of opposite hand operate on parallel shafts.
3. Bearing location indicates the direction of thrust.

7.1.2 Module

Because of the possibility of different helix angles for the gear pair, the radial modules may not be the same. However, the normal modules must always be identical.

7.1.3 Center Distance

The pitch diameter of a crossed-helical gear is given by **Equation (6-7)**, and the center distance becomes:

$$a = \frac{m_n}{2}\left(\frac{z_1}{\cos\beta_1} + \frac{z_2}{\cos\beta_2}\right) \qquad \textbf{(7-2)}$$

Again, it is possible to adjust the center distance by manipulating the helix angle. However, helix angles of both gears must be altered consistently in accordance with **Equation (7-1)**.

7.1.4 Velocity Ratio

Unlike spur and parallel shaft helical meshes, the velocity ratio (gear ratio) cannot be determined from the ratio of pitch diameters, since these can be altered by juggling of helix angles. The speed ratio can be determined only from the number of teeth, as follows:

$$\text{velocity ratio} = i = \frac{z_1}{z_2} \qquad \textbf{(7-3)}$$

or, if pitch diameters are introduced, the relationship is:

$$i = \frac{z_1 \cos\beta_2}{z_2 \cos\beta_1} \qquad \textbf{(7-4)}$$

7.2 Screw Gear Calculations

Two screw gears can only mesh together under the conditions that normal modules, m_{n1}, and, m_{n2}, and normal pressure angles, α_{n1}, α_{n2}, are the same. Let a pair of screw gears have the shaft angle Σ and helical angles β_1 and β_2:

If they have the same hands, then:
$$\Sigma = \beta_1 + \beta_2$$

If they have the opposite hands, then:
$$\Sigma = \beta_1 - \beta_2, \text{ or } \Sigma = \beta_2 - \beta_1 \qquad \textbf{(7-5)}$$

If the screw gears were profile shifted, the meshing would become a little more complex. Let β_{w1}, β_{w2} represent the working pitch cylinder;

If they have the same hands, then:
$$\Sigma = \beta_{w1} + \beta_{w2}$$

If they have the opposite hands, then:
$$\Sigma = \beta_{w1} - \beta_{w2}, \text{ or } \Sigma = \beta_{w2} - \beta_{w1} \qquad \textbf{(7-6)}$$

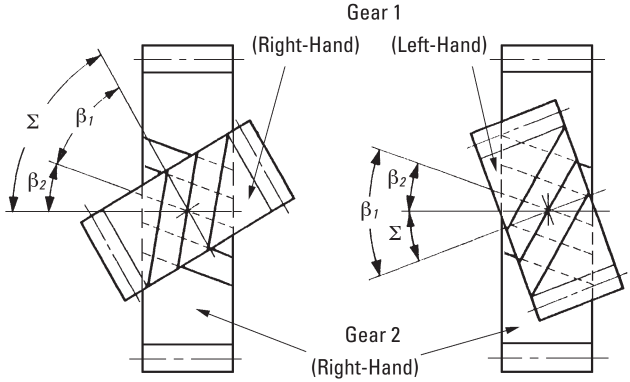

Fig. 7-2 Screw Gears of Nonparallel and Nonintersecting Axes

Table 7-1 presents equations for a profile shifted screw gear pair. When the normal coefficients of profile shift $x_{n1} = x_{n2} = 0$, the equations and calculations are the same as for standard gears.

Table 7-1 The Equations for a Screw Gear Pair on Nonparallel and Nonintersecting Axes in the Normal System

No.	Item	Symbol	Formula	Example	
				Pinion	Gear
1	Normal Module	m_n		3	
2	Normal Pressure Angle	α_n		20°	
3	Helix Angle	β		20°	30°
4	Number of Teeth & Helical Hand	z_1, z_2		15 (R)	24 (L)
5	Number of Teeth of an Equivalent Spur Gear	z_v	$\frac{z}{\cos^3\beta}$	18.0773	36.9504
6	Radial Pressure Angle	α_t	$\tan^{-1}\left(\frac{\tan\alpha_n}{\cos\beta}\right)$	21.1728°	22.7959°
7	Normal Coefficient of Profile Shift	x_n		0.4	0.2
8	Involute Function α_{wn}	inv α_{wn}	$2\tan\alpha_n\left(\frac{x_{n1}+x_{n2}}{z_{v1}+z_{v2}}\right)+\text{inv}\,\alpha_n$	0.0228415	
9	Normal Working Pressure Angle	α_{wn}	Find from Involute Function Table	22.9338°	
10	Radial Working Pressure Angle	α_{wt}	$\tan^{-1}\left(\frac{\tan\alpha_{wn}}{\cos\beta}\right)$	24.2404°	26.0386°
11	Center Distance Increment Factor	y	$\frac{1}{2}(z_{v1}+z_{v2})\left(\frac{\cos\alpha_n}{\cos\alpha_{wn}}-1\right)$	0.55977	
12	Center Distance	a_x	$\left(\frac{z_1}{2\cos\beta_1}+\frac{z_2}{2\cos\beta_2}+y\right)m_n$	67.1925	
13	Pitch Diameter	d	$\frac{zm_n}{\cos\beta}$	47.8880	83.1384
14	Base Diameter	d_b	$d\cos\alpha_t$	44.6553	76.6445
15	Working Pitch Diameter	d_{w1} d_{w2}	$2a_x\frac{d_1}{d_1+d_2}$ $2a_x\frac{d_2}{d_1+d_2}$	49.1155	85.2695
16	Working Helix Angle	β_w	$\tan^{-1}\left(\frac{d_w}{d}\tan\beta\right)$	20.4706°	30.6319°
17	Shaft Angle	Σ	$\beta_{w1}+\beta_{w2}$ or $\beta_{w1}-\beta_{w2}$	51.1025°	
18	Addendum	h_{a1} h_{a2}	$(1+y-x_{n2})m_n$ $(1+y-x_{n1})m_n$	4.0793	3.4793
19	Whole Depth	h	$[2.25+y-(x_{n1}+x_{n2})]m_n$	6.6293	
20	Outside Diameter	d_a	$d+2h_a$	56.0466	90.0970
21	Root Diameter	d_f	d_a-2h	42.7880	76.8384